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# Using diversity-based methods to estimate true epidemic sizes from sampled outbreaks

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& Cobbold (2012) derive a general expression for similarity numbers, is based on Rényi's generalised entropy and entropy. This framework reveals a coherent family of diversity indices of the *average ordinariness* of a population,

$${}^q D^{\mathbf{Z}}(\mathbf{p}) = \begin{cases} \left( \sum_{i:p_i \neq 0}^S p_i (\mathbf{Zp})_i^{q-1} \right)^{1/1-q} & \text{if } q \neq 1 \\ \prod_{i=1}^S (\mathbf{Zp})_i^{-p_i} & \text{if } q = 1 \\ (\max (\mathbf{Zp})_i)^{-1} & \text{if } q = \infty \end{cases}$$

Previous work...

order of diversity, or *viewpoint parameter*,  $q$ , determines the weight placed on a particular abundance for  $0 \leq q \leq \infty$ . Varying  $q$  allows gradients to be placed on species of differing ordinariness. Specifically,

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2001 UK FMDV  
epidemic

Di Nardo, A. 2016. *Phylodynamic modelling of foot-and-mouth disease virus sequence data.*

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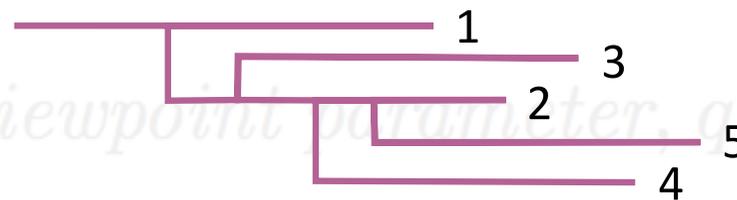


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2001 UK FMDV  
epidemic

Sequences  
generated from  
transmission tree  
mutations



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2001 UK FMDV epidemic

Sequences generated from transmission tree mutations

Phylogeny



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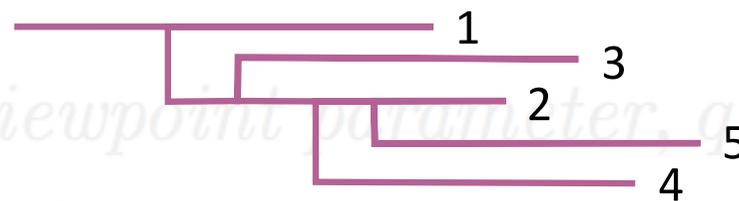
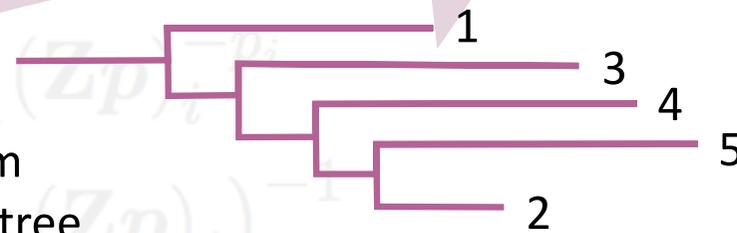


2001 UK FMDV epidemic

Sequences generated from transmission tree mutations

Phylogeny

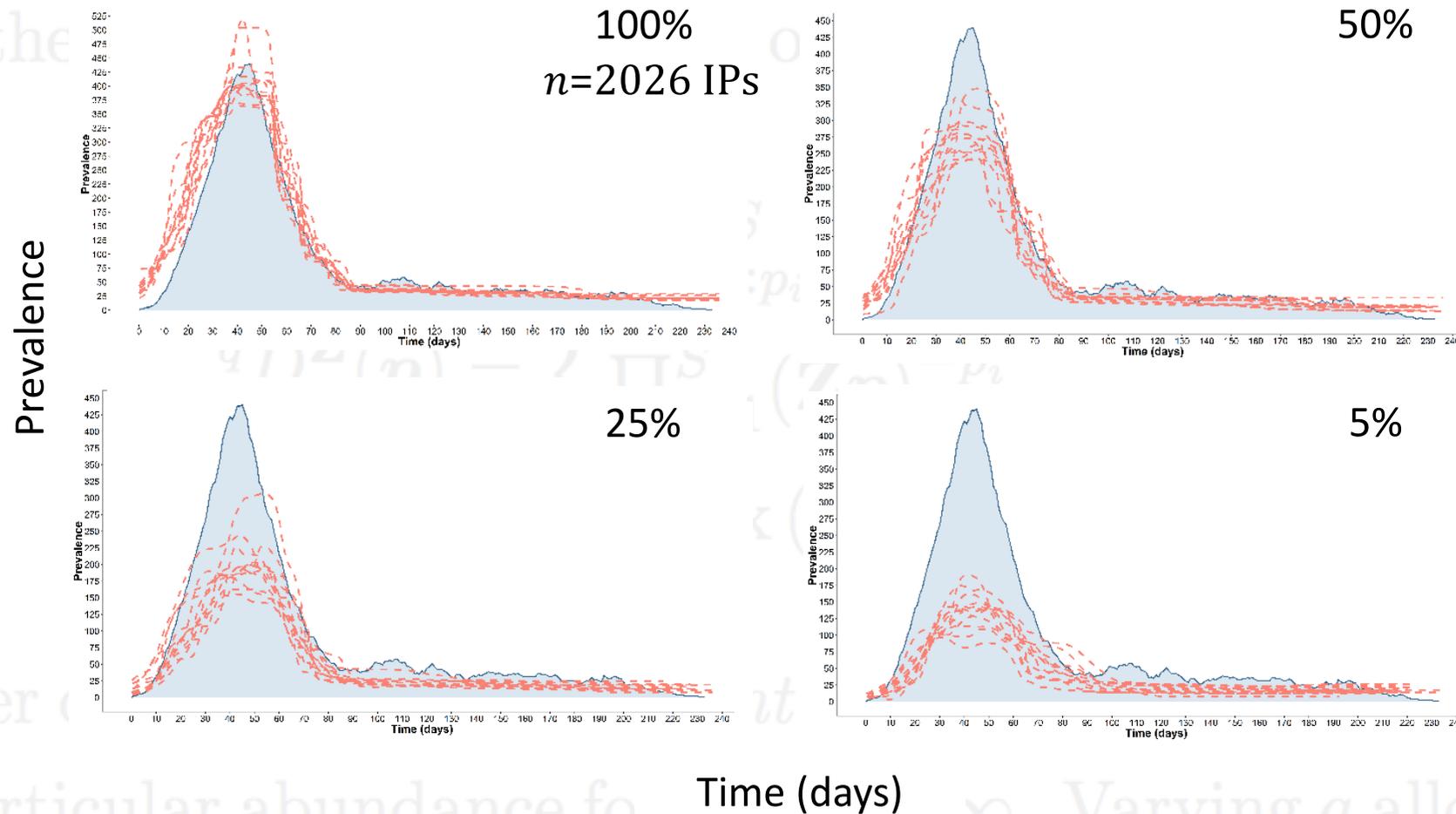
Effective population size vs. True population size



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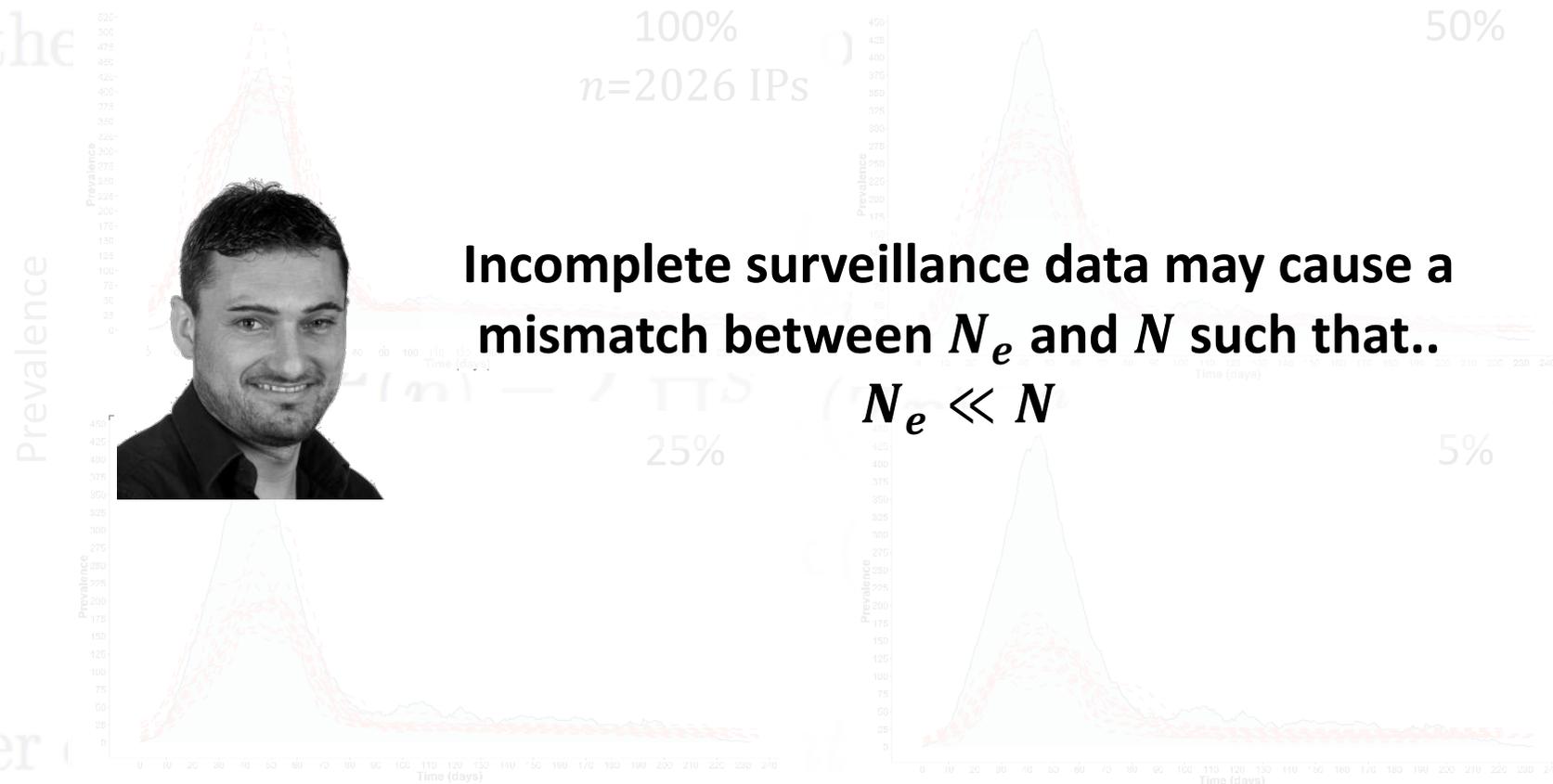
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We propose a new  
method..

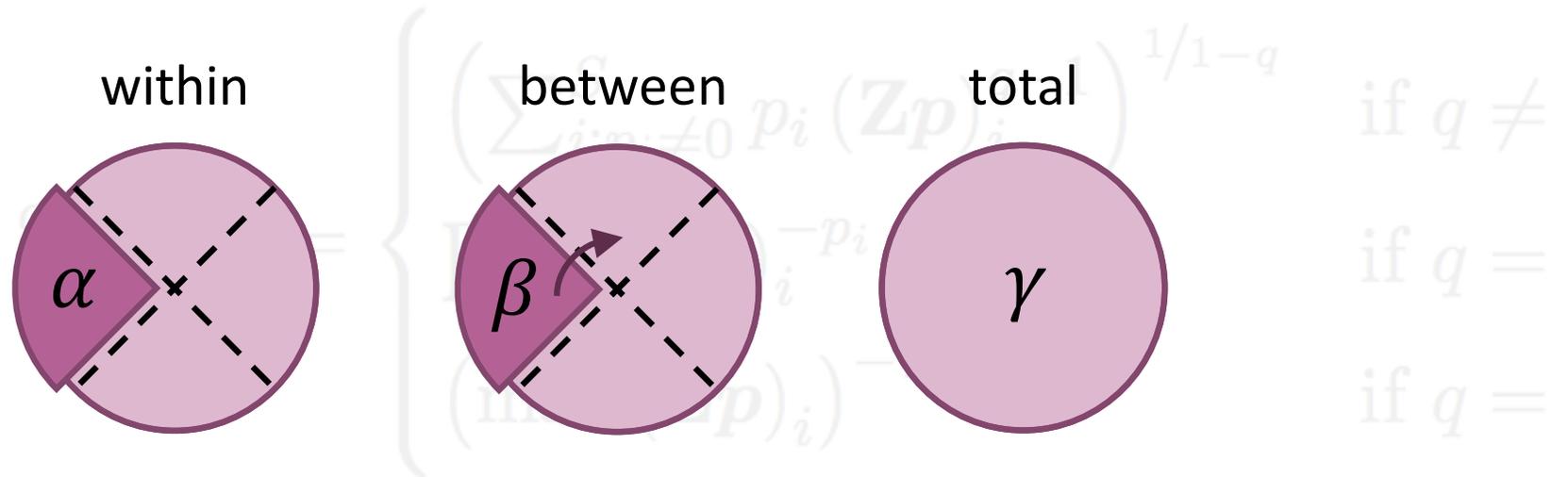
$${}^q D^Z(p) = \begin{cases} \left( \sum_{i: p_i \neq 0} p_i (Zp)_i^{q-1} \right)^{1/1-q} & \text{if } q \neq 1 \\ \prod_{i=1}^S (Zp)_i^{-p_i} & \text{if } q = 1 \\ (\max (Zp)_i)^{-1} & \text{if } q = \infty \end{cases}$$

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# Framework for Partitioning Diversity



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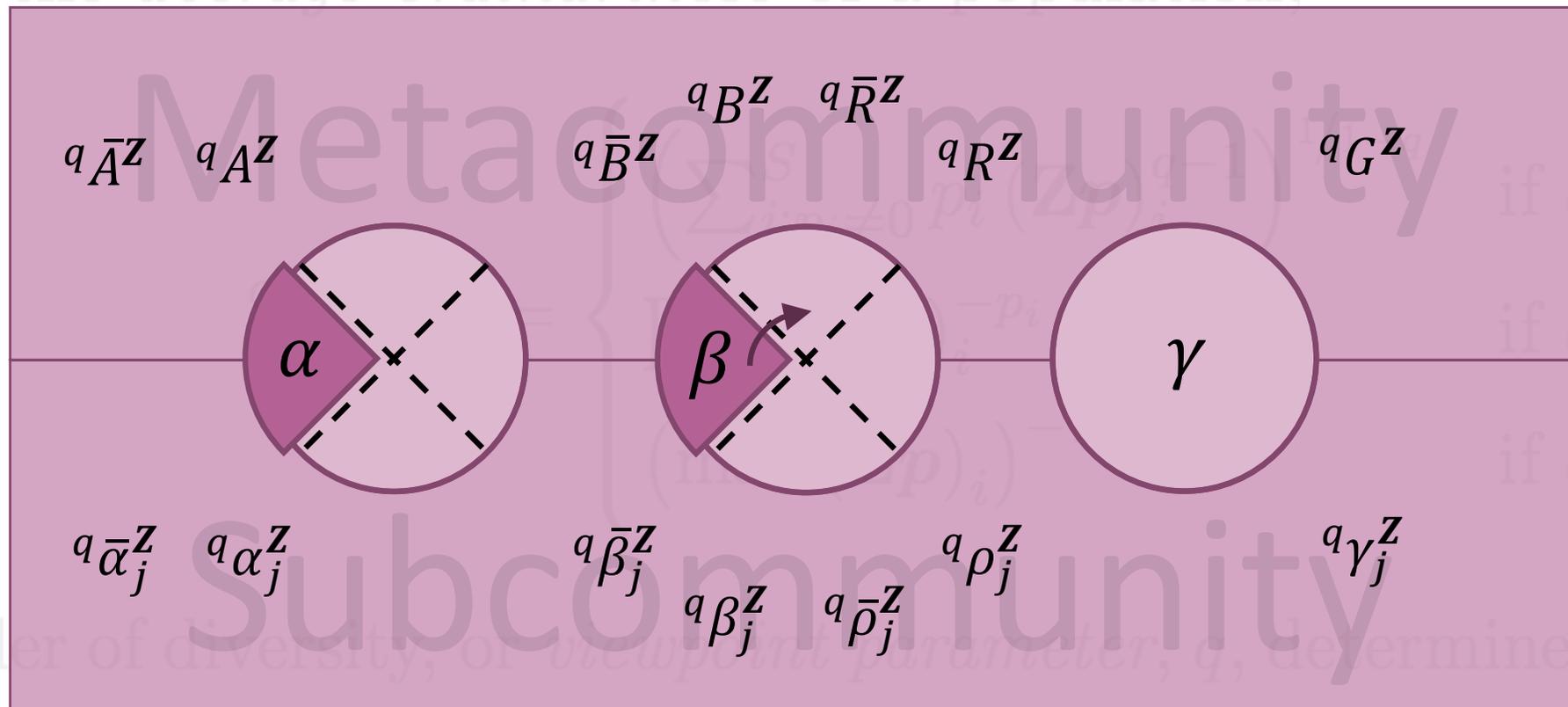


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# Framework for Partitioning Diversity



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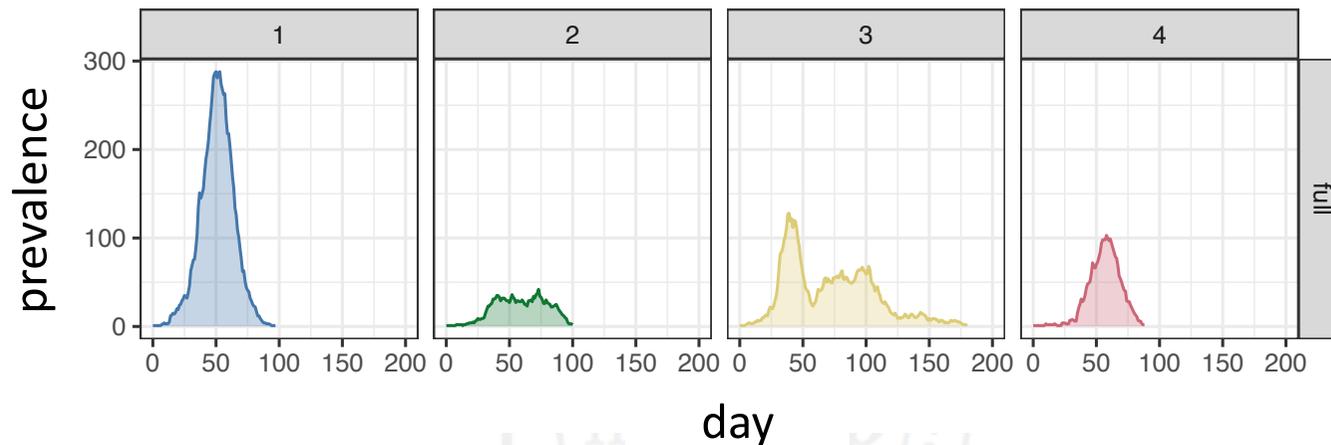


# Methods



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- Simulate outbreaks

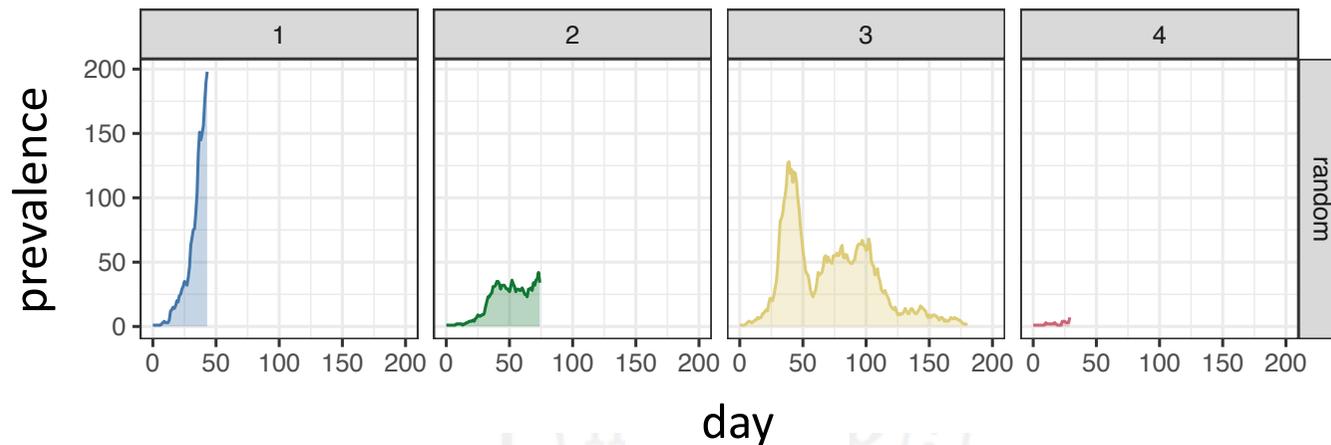


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# Methods



- Simulate outbreaks (truncated)



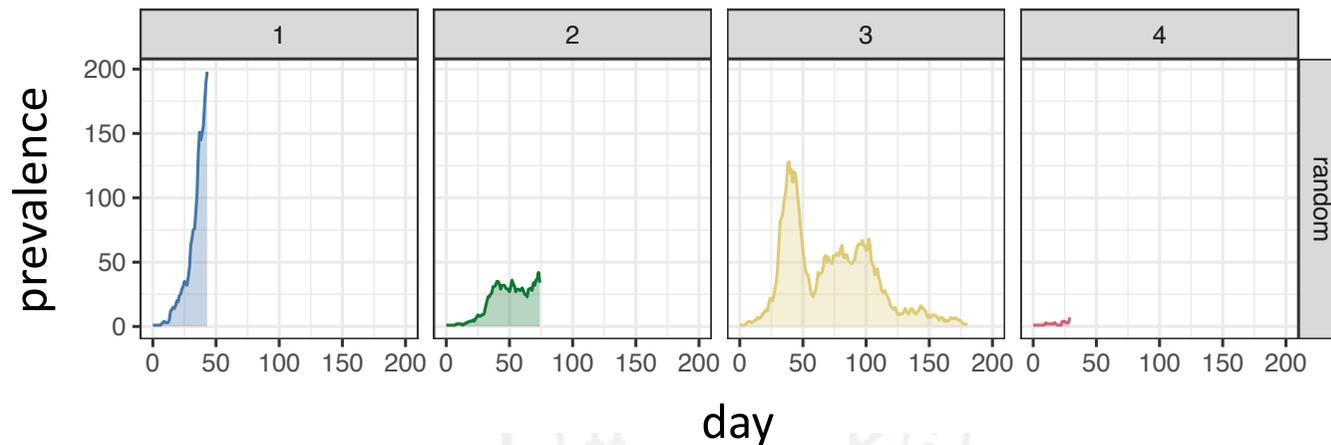
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# Methods



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- Simulate outbreaks (truncated)

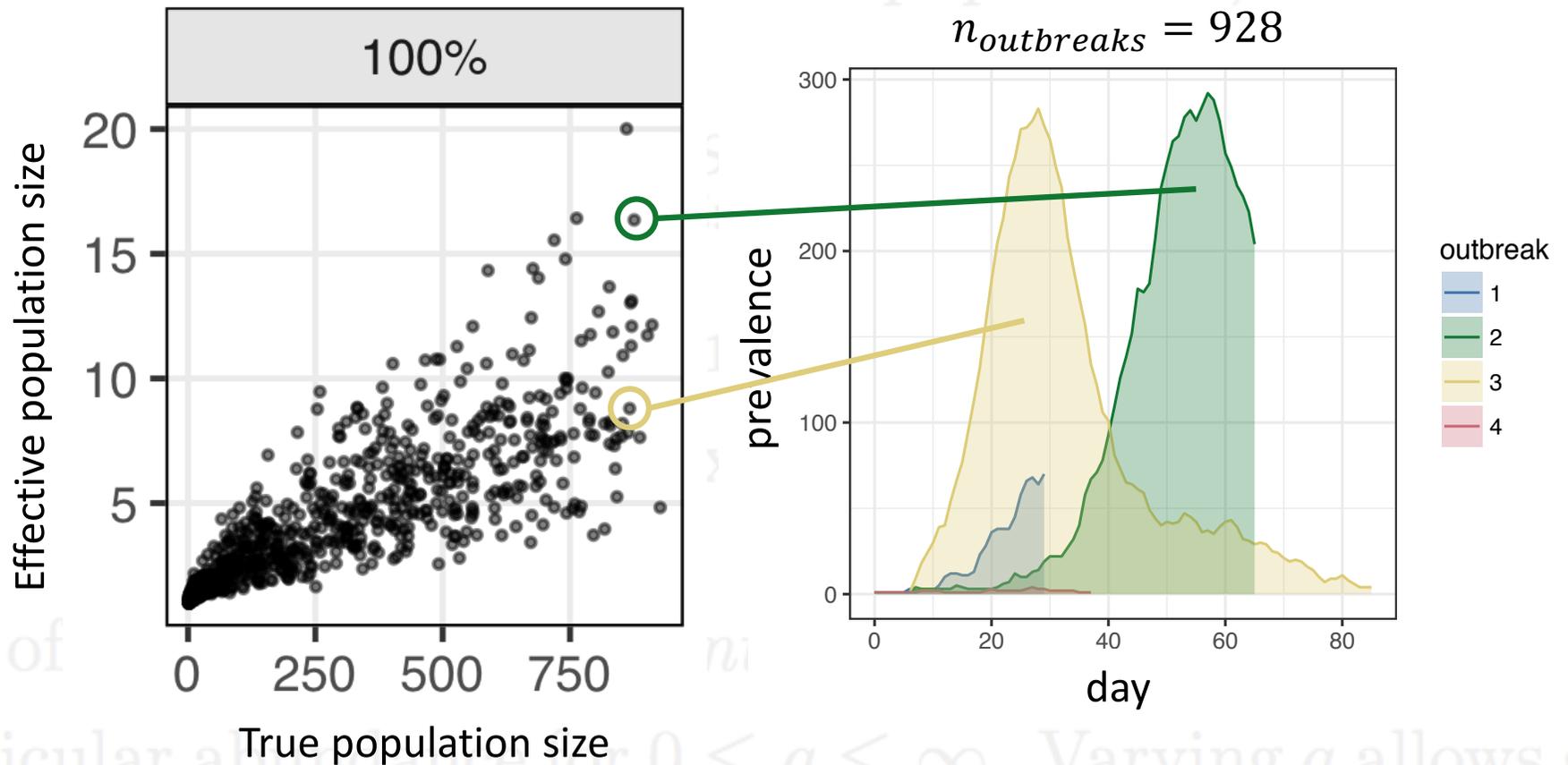


- Viral genetic diversity of the 2001 FMDV outbreak
- Calculate  ${}^qG^Z$  (Effective number of sequences / infected premises)

# Effective number of sequences, $1/G^Z$



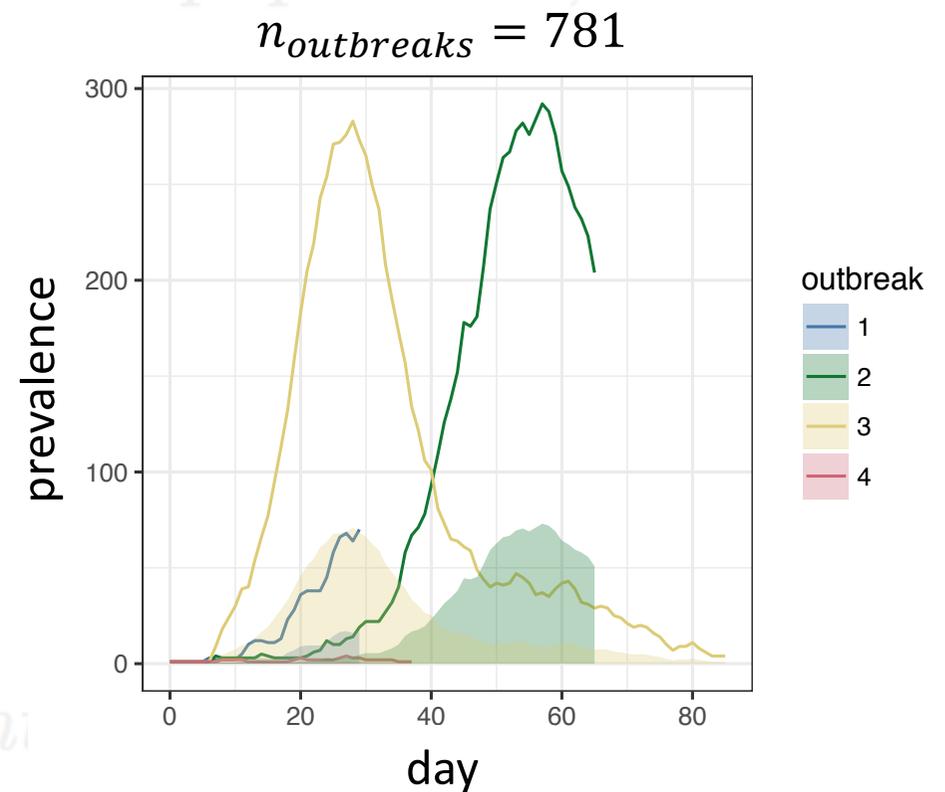
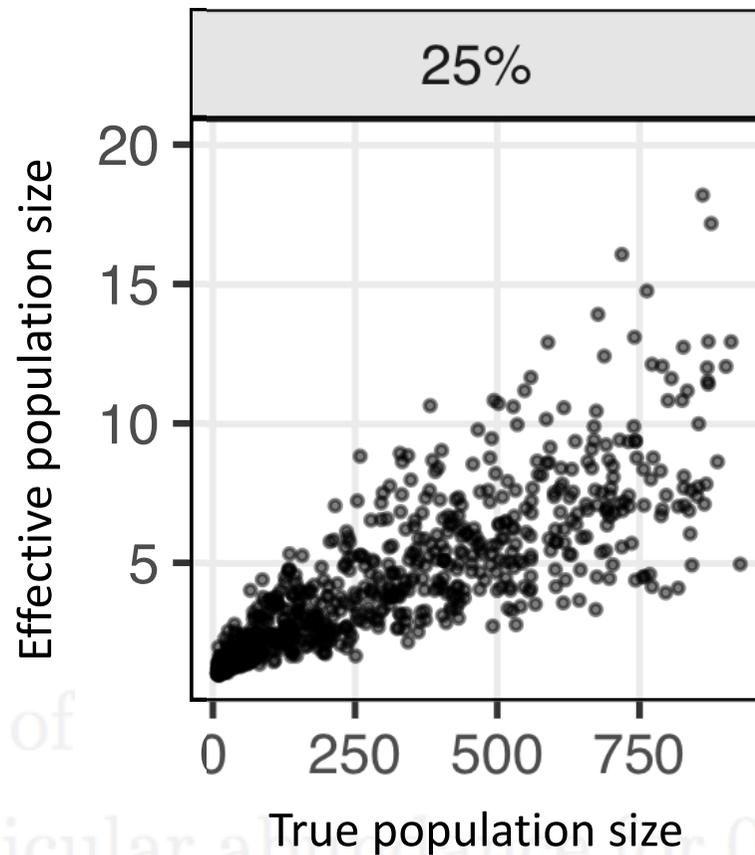
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# Effective number of sequences, $1/G^Z$



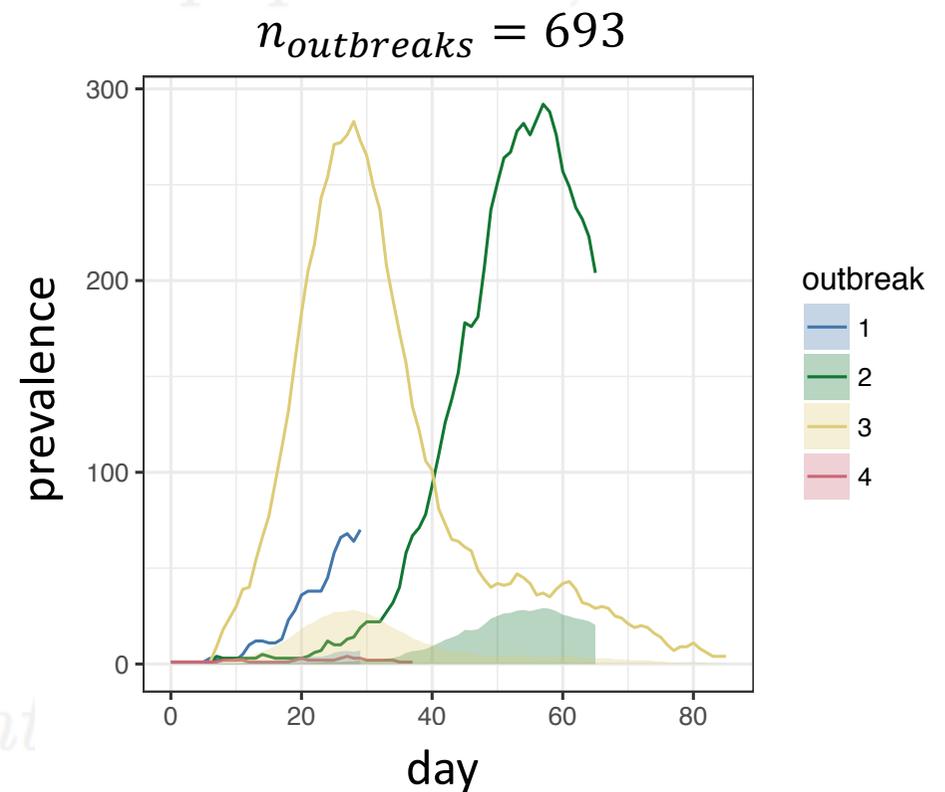
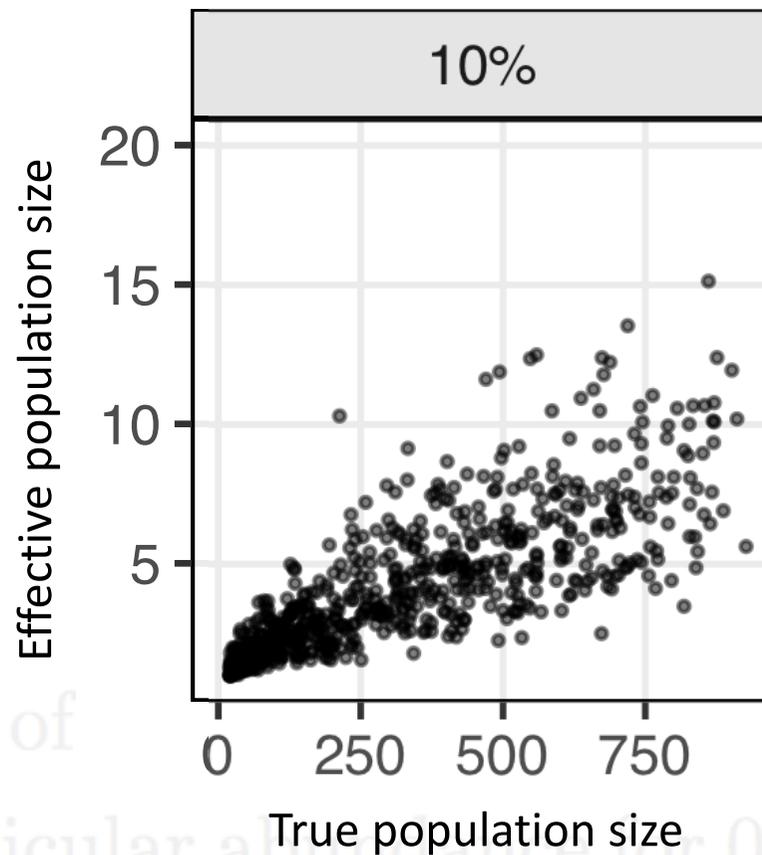
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# Effective number of sequences, $1/G^Z$



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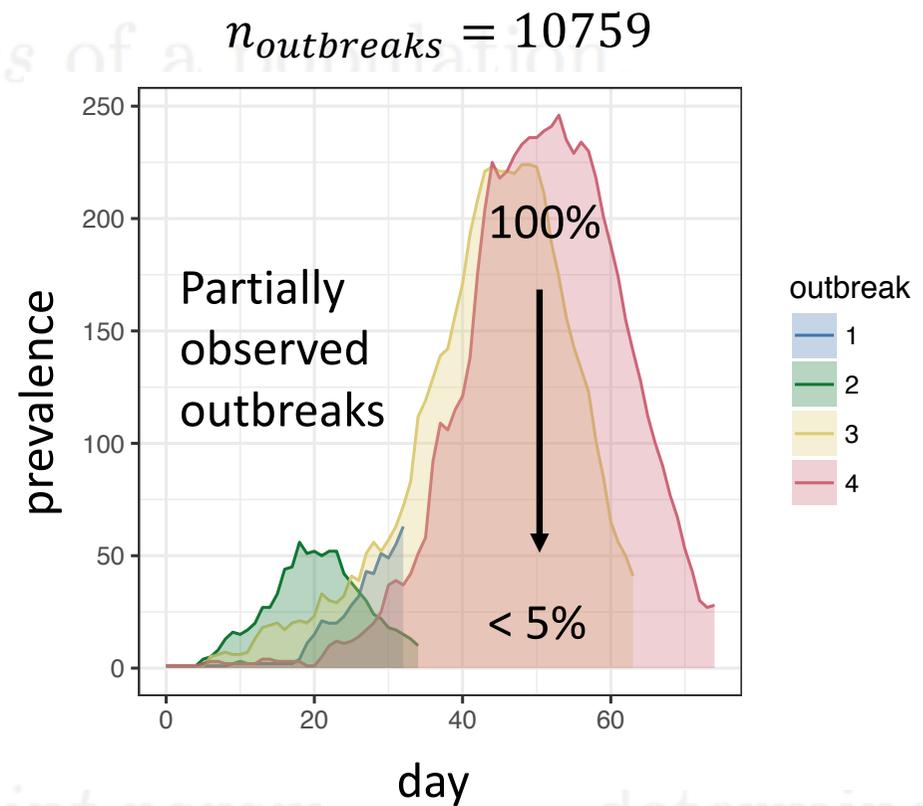
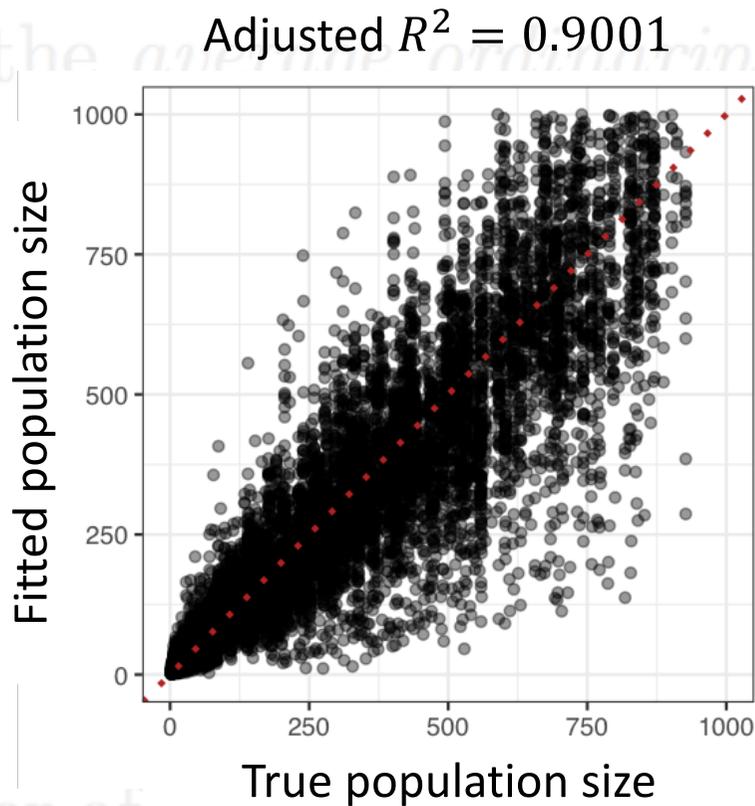


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Next, we use  ${}^q G^Z$  with  
other simple summary  
statistics..

..to fit a linear model.

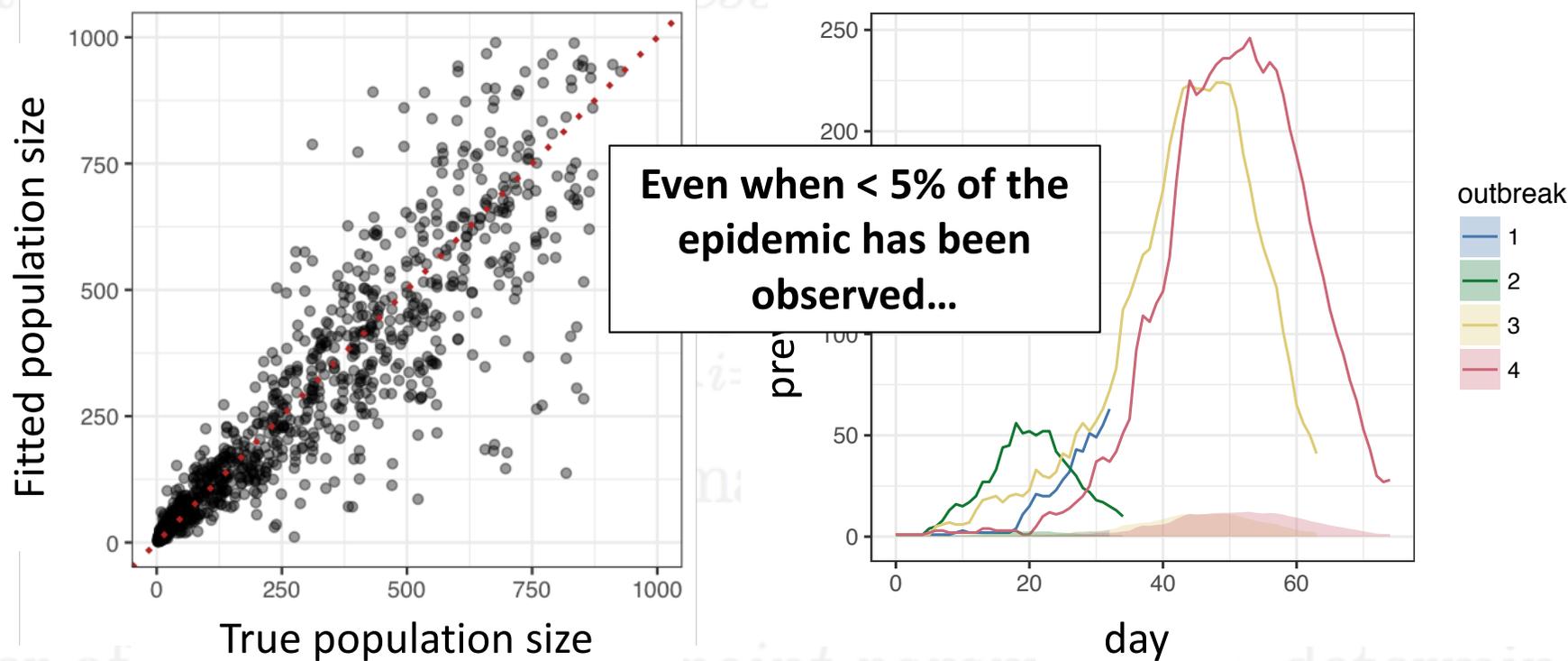
# Model fit



# Model fit



$n_{outbreaks} = 4038$



# Conclusion



- We can infer epidemic size from partially observed outbreaks
- These methods are more accurate than existing techniques

## WHAT NEXT?

- Incorporate measures of  $\beta$ -diversity
- Apply more advanced machine learning techniques, *e.g.* Google's TensorFlow



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- From the R console: `install.packages('rdiversity')`
- Reeve, R. et al. (2016). *How to partition diversity*. arXiv:1404.6520 [q-bio.QM].
- Di Nardo, A. 2016. *Phylogenetic modelling of foot-and-mouth disease virus sequence data*. [PhD Thesis]



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